

Time Value of Money

#	TVM Formula For:	Annual Compounding	Compounded (m) Times per Year	Continuous Compounding
1	Future Value of a Lump Sum. (FVIF_{r,n})	$FV = PV(1+r)^n$	$FV = PV\left(1 + \frac{r}{m}\right)^{n*m}$	$FV = PV(e)^{r*n}$
2	Present Value of a Lump Sum. (PVIF_{r,n})	$PV = FV(1+r)^{-n}$	$PV = FV(1 + k/m)^{-nm}$	$PV = FV(e)^{-r*n}$
3	Future Value of an Ordinary Annuity. (FVIFA_{r,n})	$FVA = PMT \left[\frac{(1+r)^n - 1}{r} \right]$	$FVA = PMT \left[\frac{\left(1 + \frac{r}{m}\right)^{n*m} - 1}{\frac{r}{m}} \right]$	
4	Future Value of an Annuity Due. (FVIFA_{r,n})	$FVA = PMT \left[\frac{(1+r)^n - 1}{r} \right] (1+r)$	$FVA = PMT \left[\frac{\left(1 + \frac{r}{m}\right)^{n*m} - 1}{\frac{r}{m}} \right] \left(1 + \frac{r}{m}\right)^m$	
5	Present Value of an Annuity. (PVIFA_{r,n})	$PVA = PMT \left[\frac{1 - (1+r)^{-n}}{r} \right]$	$PVA = PMT \left[\frac{1 - \left(1 + \frac{r}{m}\right)^{-n*m}}{\frac{r}{m}} \right] \left(1 + \frac{r}{m}\right)^m$	
6	Present Value of an Annuity Due. (PVIFA_{r,n})	$PVA = PMT \left[\frac{1 - (1+r)^{-n}}{r} \right] (1+r)$	$PVA = PMT \left[\frac{1 - \left(1 + \frac{r}{m}\right)^{-n*m}}{\frac{r}{m}} \right] \left(1 + \frac{r}{m}\right)^m$	
7	Present Value of Perpetuity. (PV_p)	$PV_{\text{perpetuity}} = \frac{PMT}{r}$	$PV_{\text{perpetuity}} = \frac{PMT}{\left[\left(1 + \frac{r}{m}\right)^m - 1\right]}$	
8	Effective Annual Rate given the APR.	$EAR = APR$	$EAR = \left(1 + \frac{r_{\text{nominal}}}{m}\right)^m - 1$	$EAR = e^r - 1$
9	The length of time required for a PV to grow to a FV. (Lump Sum)	$n = \frac{\ln(FV/PV)}{\ln(1+r)}$	$n = \frac{\ln(FV/PV)}{m * \ln\left(1 + \frac{r}{m}\right)}$	$n = \frac{\ln(FV/PV)}{r}$
10	The APR required for a PV to grow to a FV. (Lump Sum)	$r = \left(\frac{FV}{PV}\right)^{1/n} - 1$	$r = m * \left[\left(\frac{FV}{PV}\right)^{1/(n*m)} - 1\right]$	$r = \frac{\ln(FV/PV)}{n}$
11	Present Value of a Growing Annuity.	$PV = \frac{CF_0(1+g)}{(r-g)} \left[1 - \left(\frac{1+g}{1+r}\right)^n \right]$		
12	The length of time required for a series of PMT's to grow to a future amount (FVA_n). (Ordinary Annuity)	$n = \frac{\ln\left[\frac{(FVA)(r)}{PMT} + 1\right]}{\ln(1+r)}$	$n = \frac{\ln\left[\left(\frac{r}{m}\right)\left(\frac{FVA}{PMT} + \frac{m}{r}\right)\right]}{m * \ln(1+r/m)}$	
13	The length of time required for a series of PMT's to exhaust a specific present amount (PVA_n). (Ordinary	$n = -\frac{\ln\left[1 - \frac{(PVA)(r)}{PMT}\right]}{\ln(1+r)}$	$n = -\frac{\ln\left[1 - \frac{(PVA)(r/m)}{PMT}\right]}{m * \ln(1+r/m)}$	

	Annuity	for $PVA(r) < PMT$	for $PVA(r/m) < PMT$	
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Bond Valuation			
#	Formula For:	Annual	Semiannual Payments
1	Interest	$INT = CR * m$	$INT = \frac{CR}{2} * m$
2	Bond Valuation	$V_B = INT \left(\frac{1 - (1 + r_d)^{-n}}{r_d} \right) + \frac{M}{(1 + r_d)^n}$	$V_B = \frac{INT}{2} \left(\frac{1 - \left(1 + \frac{r_d}{2}\right)^{-2n}}{\frac{r_d}{2}} \right) + \frac{M}{\left(1 + \frac{r_d}{2}\right)^{2n}}$
3	Determining Coupon Rate	$V_B = INT \left(\frac{1 - (1 + r_d)^{-n}}{r_d} \right) + \frac{M}{(1 + r_d)^n}$ $INT = CR * M$	$V_B = \frac{INT}{2} \left(\frac{1 - \left(1 + \frac{r_d}{2}\right)^{-2n}}{\frac{r_d}{2}} \right) + \frac{M}{\left(1 + \frac{r_d}{2}\right)^{2n}}$ $INT = CR * M$
4	Yield to Maturity	$YTM = \frac{INT + \left(\frac{M - V_B}{n}\right)}{\left(\frac{M + 2V_B}{3}\right)}$	$YTM = \frac{INT + \left(\frac{M - V_B}{2n}\right)}{\left(\frac{M + 2V_B}{3}\right)}$ $YTM = YTM * 2$
5	Yield to Call	$YTM = \frac{INT + \left(\frac{Call Price - V_B}{n}\right)}{\left(\frac{Call Price + 2V_B}{3}\right)}$	$YTM = \frac{INT + \left(\frac{Call Price - V_B}{2n}\right)}{\left(\frac{Call Price + 2V_B}{3}\right)}$ $YTM = YTM * 2$
6	Current Yield	$\frac{INT_s}{Current Price}$	

Stock Valuation		
#	Formula For:	
1	Preferred Stock	$V_{ps} = \frac{\text{preferred dividend}}{\text{required rate of return}} = \frac{D_{ps}}{r_{ps}}$
2	Common Stock (Zero Growth)	$P_0 = \frac{D}{r_s}$
3	Common Stock (Constant Growth)	$P_0 = \frac{D_0(1+g)}{r_s - g} = \frac{D_1}{r_s - g}$
4	Dividends	$D_1 = D_0(1+g)$ or $D_2 = D_0(1+g)^2 = D_1(1+g)$ or $D_3 = D_0(1+g)^3 = D_1(1+g)^2 = D_2(1+g)$
5	Common Stock (Constant Growth for a given # of years)	$P_0 = \frac{D_1}{r_s - g} \left[1 - \left(\frac{1+g}{1+r_s}\right)^n \right]$
6	Required Rate of Return	$r_s = \frac{Div_1}{P_0} + g$

Risk and Return			
	Formula For:	Single Security	Portfolio
1	Expected Return	$\hat{r} = \sum_{i=1}^n P_i r_i$	$\hat{r}_p = \sum_{i=1}^N W_i \hat{r}_i$ $\hat{r}_p = W_1 \hat{r}_1 + W_2 \hat{r}_2 + \dots + W_N \hat{r}_N$ <p>or</p> $SML = r_s = r_{RF} + (r_M - r_{RF})b_i$
2	Variance	$\sigma_i^2 = \sum_{j=1}^m P_{ij} (r_{ij} - \hat{r}_i)^2$	$\sigma_p^2 = W_1^2 \sigma_1^2 + W_2^2 \sigma_2^2 + 2 W_1 W_2 \sigma_{12}$ covariance $\sigma_p^2 = W_1^2 \sigma_1^2 + W_2^2 \sigma_2^2 + 2 W_1 W_2 \sigma_1 \sigma_2 \rho_{12}$ correlation
3	Std. Deviation	$\sigma = \sqrt{\sigma_i^2}$	$\sigma = \sqrt{\sigma_p^2}$
4	Coefficient of Variation	$CV = \frac{\sigma}{\hat{r}}$	
5	Covariance	$\sigma_{12} = \sum_{j=1}^M P_i (r_{1j} - \hat{r}_1)(r_{2j} - \hat{r}_2)$	
6	Correlation	$\rho_{12} = \frac{\sigma_{1,2}}{\sigma_1 * \sigma_2}$	
7	Beta	$b = \frac{\sigma_{1m}}{\sigma_m^2}$	$b_p = W_1 b_1 + W_2 b_2 + \dots + W_n b_n$

Capital Budgeting		
	Formula For:	
1	Net Present Value (NPV)	$NPV = -CF_0 + \sum_{t=1}^n \frac{CF_t}{(1+r)^t}$
2	Internal Rate of Return (IRR)	$-CF_0 + \sum_{t=1}^n \frac{CF_t}{(1+IRR)^t} = 0$ <p>or</p> $IRR = \frac{\text{Cash Flow}}{\text{Cost}}$
3	Modified Internal Rate of Return (MIRR)	$MIRR = \left(\frac{TV}{PV \text{ Cost}} \right)^{(1/n)} - 1$
4	Payback Period	$\text{Payback period} = \frac{\text{net cash flows}}{\text{annual net cash inflow}}$ <p>or</p> $\text{Payback period} = \text{year before full recovery} + \frac{\text{uncovered cost at start of year}}{\text{cash flow during year}}$
5	Equivalent Annual Annuity (EAA)	$EAA = \frac{NPV}{\left(\frac{1 - (1+r)^{-n}}{r} \right)}$

Cost of Capital

	Formula For:	Without Flotation Cost	With Flotation Cost
1	Cost of Debt (rd)	$r_d = \text{YTM} = \frac{INT + \left(\frac{M - Vb}{N}\right)}{\left(\frac{M + 2V_B}{3}\right)}$	
2	Cost of Preferred Equity (rp)	$r_p = \frac{D_p}{P_n}$	$r_p = \frac{D_p}{P_n(1 - F)}$ if F in % or $r_p = \frac{D_p}{P_n - F_s}$ if F in \$
3	Cost of Retained Earnings (rs)	<p>CAPM Approach - $r_s = r_{RF} + (r_M - r_{RF})b_i$</p> <p>Discounted Cash Flow Approach (DCF) $r_s = \frac{D_1}{P_0} + g$</p> <p>Bond Yield + Risk Premium Approach Bond Yield + Risk Premium</p>	
4	Cost of Newly Issued Common Stock (re)		$r_e = \frac{D_1}{P_0(1 - F)} + g$
5	Weighted Average Cost of Capital (WACC)	$\text{WACC} = W_d r_d (1 - T) + W_p r_p + W_s r_s$	

Legend

r = the nominal rate, component cost of capital, discount rate, Annual Percentage Rate (APR)	PMT = the periodic payment or cash flow
m = the number of compounding periods per year	EAR = the Effective Annual Rate
\ln = the natural logarithm, the logarithm to the base e	e = the base of the natural logarithm ≈ 2.71828
PMT = the periodic payment or cash flow	n = the number of periods
CR = coupon rate, %	M = maturity value, par value
INT = Interest, \$	Vb = Value of the bond
P_0 = Price today	r_d = cost of debt, rate of return required by bondholders
r_s = required rate of return by stockholders	D = dividend
F = Flotation Cost	g = growth rate
b = beta	P_i = probability
ρ_{12} = correlation	$\sigma_{1,2}$ = covariance
\hat{r} = expected return	σ_i^2 = variance and σ_i = standard deviation
TV = Terminal Value, FV of all cash inflows	W = proportion invested